Model Question Paper Fourth Semester B. Tech Degree Examination (2013 scheme)

13.406 Formal Languages & Automata Theory

Time: 3 Hrs

Max. Marks: 100

Part-A

Answer all questions.

1. Define 2DFA, with example. How does it differ from DFA?

2. Is the language $\{0^{2n} \mid n \ge 1\}$ regular? Justify.

- 3. Suppose δ is the transition function of a DFA. Prove that for any input strings x and y, $\delta(q, xy) = \delta(\delta(q, x), y)$.
- 4. Let G be the grammar $S \to aS \mid aSbS \mid \epsilon$. Prove that $L(G) = \{x \mid each \text{ prefix of } x \text{ has at least as many } a's as b's \}$.
- 5. Define Turing machine. What are its uses?

 $(5 \times 4 = 20 \text{ marks})$

Part-B

Answer one full question from each module.

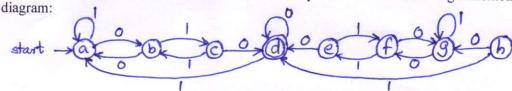
Module I

- 6. a) Construct the DFA equivalent to the following NFA. $M=(\{q_0, q_1\}, \{0, 1\}, \delta, q_0, \{q_1\})$ and $\delta(q_0, 0) = \{q_0, q_1\}, \delta(q_0, 1) = \{q_1\}, \delta(q_1, 0) = \phi, \delta(q_1, 1) = \{q_0, q_1\}.$
 - b) Define Moore machine. Design a Moore machine to output residue mod 4(remainder of the input number when divided by 4) for binary input string treated as binary integer.
- 7. a) With the help of an example, explain how a Mealy machine is transformed to equivalent Moore machine.
 - b) Construct NFA without ϵ transitions from the following NFA. $M=(\{q_0, q_1, q_2\}, \{0, 1, 2\}, \delta, q_0, \{q_2\})$ and $\delta(q_0, 0) = \{q_0\}, \delta(q_0, \epsilon) = \{q_1\}, \delta(q_1, 1) = \{q_1\}, \delta(q_1, \epsilon) = \{q_2\}, \delta(q_2, 2) = \{q_2\}.$

Module II

- 8. a) Write regular expressions for each of the following languages over the alphabet {0, 1}.

 i) The set of all strings with at most one pair of consecutive 0's and at most one pair
 - i) The set of all strings with at most one pair of consecutive 0's and at most one pair of consecutive 1's.
 - ii) The set of all strings not containing 101 as a substring.
 - b) Find the minimum state finite state automaton equivalent to the following transition



- 9. a) Construct finite automata(NFA) equivalent to the regular expression: $01[((10)^* + 11)^* + 0]^*1$
 - b) Construct regular expressions corresponding to the following state diagram:

